

Types of Matrices :

① Row matrix: A matrix having only 1 row and n columns.

$$[3 \quad 4 \quad 5 \quad 6]$$

② Column matrix: A matrix having only 1 column and n rows

$$\begin{bmatrix} 2 \\ 3 \\ 8 \\ 7 \end{bmatrix}$$

③ Null Matrix: If all entries are zero, the matrix is called a zero or null matrix.

④ Square matrix: If the number of rows = the number of columns, the matrix is called a square matrix.

⑤ Diagonal Matrix: If A is a square matrix, where all non-diagonal elements are 0, then A is called a diagonal matrix.

$$\begin{bmatrix} 7 & 0 & 0 \\ 0 & 9 & 0 \\ 0 & 0 & 3 \end{bmatrix}$$

⑥ Scalar Matrix: A matrix having same scalar on the diagonal is called a scalar matrix. i.e. when the elements of diagonal are same.

$$\begin{bmatrix} 5 & 0 & 0 \\ 0 & 5 & 0 \\ 0 & 0 & 5 \end{bmatrix}$$

Every scalar matrix is

- (1) diagonal matrix (2) square matrix

Every diagonal matrix is a square matrix

(7) Identity matrix: If A is a diagonal matrix, where all the diagonal elements are 1, then A is called an identity matrix / unit matrix. It is denoted by 'I' or 'U'.

$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

When the identity matrix is multiplied by any other matrix, the result will be the same matrix.

(8) Diagonal matrix: When only the non diagonal elements are zero, the matrix is called diagonal matrix.

$$\begin{bmatrix} 4 & 0 & 0 \\ 0 & 5 & 0 \\ 0 & 0 & 6 \end{bmatrix}$$

(9) Triangular matrix:

$$\begin{bmatrix} 1 & 0 & 0 \\ 3 & 7 & 0 \\ 4 & 5 & 9 \end{bmatrix}$$

upper triangular matrix

$$\begin{bmatrix} 1 & 3 & 4 \\ 0 & 7 & 5 \\ 0 & 0 & 6 \end{bmatrix}$$

lower triangular matrix

(i) **Symmetric matrix:** A matrix such that $a_{ij} = a_{ji}$ for all i, j in the matrix

$$\begin{array}{c}
 \begin{array}{ccc}
 & \begin{array}{c} a_{11} \\ \downarrow \\ 1 \end{array} & \begin{array}{c} a_{12} \\ \downarrow \\ 7 \end{array} & \begin{array}{c} a_{13} \\ \downarrow \\ 3 \end{array} \\
 \begin{array}{c} a_{21} \\ \rightarrow \end{array} & 7 & 9 & 4 \\
 \begin{array}{c} a_{31} \\ \rightarrow \end{array} & 3 & 4 & 6 \\
 & & \begin{array}{c} \uparrow \\ a_{32} \end{array} & \begin{array}{c} \uparrow \\ a_{33} \end{array}
 \end{array}
 \end{array}
 \end{array}$$

The transpose of the matrix is the same as the matrix

(ii) **Skew Symmetric matrix:**

$$X = \begin{bmatrix} 0 & 3 & 4 \\ -3 & 0 & 7 \\ -4 & -7 & 0 \end{bmatrix}$$

$$\text{negative } a_{ij} = -a_{ji}$$

Transpose of a matrix is equal to the matrix